

## R1-2002 Q1(g)

- g) A neutron moving through heavy water strikes, head on, an isolated stationary deuteron.
- Assuming the mass  $m$  of the neutron is equal to half that of the deuteron, show that the ratio of the final speed of the deuteron,  $v_d$ , to the incident speed of the neutron,  $u_n$ , is  $\left(\frac{2}{3}\right)$ .
  - Determine the percentage of the initial kinetic energy acquired by the deuteron.
  - How many such collisions would be required to slow the neutron down from 10 Mev to 0.01 ev?

[16]

## R1-2003 Q1(c)

- c) A rocket, of constant mass  $2.00 \times 10^3$  kg, is fired vertically upwards with constant acceleration. After one minute it reaches a height of 36.0 km and its engine is switched off. Assuming the rocket's mass and  $g$  remain constant, calculate:
- the initial acceleration of the rocket
  - the maximum height reached
  - the total time of flight
  - the work done by the rocket

Why is the assumption made unrealistic?

[10]

### R1-2003 Q1(g)

- g) A puck of mass  $m$ , velocity  $v$ , coordinates  $(x,y)$ , slides under gravity, without friction, on the smooth track shown in Figure 1.2. Determine, or answer, the following:

- (i) the acceleration  $f$  along the straight portion of the track
- (ii) the total energy  $E$  of the puck when located at  $(x,y)$
- (iii) comment on the resultant acceleration at 0
- (iv) if released from rest at  $x = a$ , determine its velocity at 0. [5]

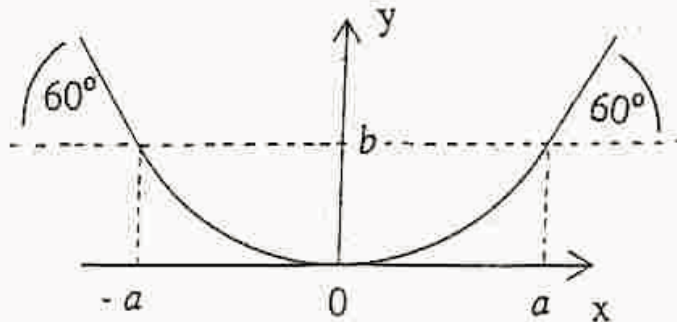


Figure 1.2

### R1-2004 Q1(i)

- i) A lady ice skater, mass 60 kg, is moving at  $12 \text{ m s}^{-1}$  in a straight line. She decelerates by standing on one skate, and comes to rest in 40 m. Neglecting air resistance, calculate:

- (i) her deceleration
  - (ii) the coefficient of friction between the skate and the ice
  - (iii) her loss of kinetic energy
  - (iv) the maximum mass of ice melted [8]
- The specific latent heat of melting of ice is  $330 \text{ kJ kg}^{-1}$ .

## R1-2004 Q1(n)

- n) During a thunder storm a student sets his stopwatch to zero at the time of a lightning strike. He records the time,  $t$ , of a subsequent lightning strike, from the same direction, and the time interval,  $\Delta t$ , between each strike and the following thunder clap. His results are given in the table below.

$t/s$	$\Delta t/s$
0	32.5
49.1	18.0

- (i) Why does the lightning strike occur before the thunder clap?
- (ii) Determine the speed  $u$  at which the storm is approaching.

Assume the speed of sound is  $334 \text{ m s}^{-1}$ .

[6]

## R1-2005 Q1(f)

- f) A bullet leaves the 1.20 m barrel of a rifle at a horizontal speed of  $310 \text{ m s}^{-1}$ :
- (i) Calculate the acceleration of the bullet in the barrel assuming it to be constant.
  - (ii) If the bullet emerges from the barrel after two complete rotations, estimate its final rotational speed in radians per second.
  - (iii) What advantage has a barrel that causes the bullet to rotate?
  - (iv) In practice the acceleration of the bullet is not constant. Sketch a graph of the expected variation, with distance, and explain the variation.

[5]

## R1-2005 Q1(h)

h) The acceleration,  $a$ , of a particle, velocity  $v$ , along a straight line can have the following forms:

- (i)  $g$
- (ii)  $g - kv$
- (iii)  $-\omega\sqrt{b^2\omega^2 - v^2}$ ,

$g$  is the constant acceleration of free fall,  $v$  is the velocity,  $k$ ,  $\omega$  and  $b$  are constants. Sketch graphs, for each case, assuming  $v = 0$  at time  $t = 0$ , of:

- (1)  $a$  against  $v$
- (2)  $v$  against time,  $t$ .

[8]

## R1-2005 Q1(l)

Two identical elastic spheres, each of mass  $m$ , are at rest on a smooth table and touch each other. They are struck symmetrically by an identical sphere, but of mass  $M$ , having a velocity  $u$ , perpendicular to the line of centres of the two stationary spheres. The mass  $M$  comes to rest immediately after the collision.

Determine the ratio  $M/m$ .

[4]

## R1-2006 Q1(m)

(m) A car starts from rest at time  $t = 0$  and travels with constant acceleration  $a_1$  for time  $t_1$ . From time  $t_1$  to  $t_2$  it travels with constant speed  $\bar{u}$ . After  $t_2$  a retarding acceleration is applied, of initial magnitude  $a_2$ , which decreases linearly to zero at time  $t_3$  when the car comes to rest.

Sketch the following graphs:

- (i) acceleration – time
- (ii) velocity – time
- (iii) distance – time

[3]

### R1-2007 Q1(m)

(m) A 0.20 kg mass is attached to the lower end of a helical spring which is fixed at its upper end. The vertical spring is extended by 0.16 m when in equilibrium. Determine :

- (i) the change in gravitational potential energy of the mass due to the spring's extension
- (ii) the elastic energy stored in the spring
- (iii) Why do the magnitudes of (i) and (ii) differ ?

The mass is pulled down a further distance of 0.08 m and released.

- (iv) What is its kinetic energy when passing through the equilibrium position ?
- (v) What is its period of oscillation ?
- (vi) If the upper end of the spring is released, describe the motion of the mass and the spring. [10]

### R1-2008 Q1(f)

(f) A vehicle is travelling at 60 mph along a straight road, without slipping. What are the velocities at the 'compass points', N, S, E, and W, of the rim of the wheel ? [7]

### R1-2009 Q1(d)

(d) A man cycles to work, with the wind behind him, at  $8.0 \text{ ms}^{-1}$  and returns home, Against the wind, at  $4.0 \text{ ms}^{-1}$ . What is his average speed ? [3]

### R1-2009 Q1(k)

(k) Answer the following questions with an example where possible:

- (i) Can a body be accelerating while travelling at constant speed ?
- (ii) Can a body have a constant velocity and a varying speed ?
- (iii) If a body has zero velocity, can it be accelerating ?
- (iv) Can a body be accelerating in a direction opposite to its velocity ?

[6]

### R1-2010 Q1(I)

- (1) A boat can travel at a speed of  $3.0 \text{ ms}^{-1}$  on a pond. A boatman wants to cross a river by the shortest path. In what direction should he row, with respect to the bank, if the speed of the water is  $2.0 \text{ ms}^{-1}$ .

Explain, using a diagram, which path he should take if the water speed is  $4.0 \text{ ms}^{-1}$ . [7]

### R1-2011 Q1(i)

- i) A sphere, mass  $M$  and speed  $u$ , collides elastically head-on with an identical sphere of mass  $m$  which is initially at rest. After the collision the masses  $M$  and  $m$  have respectively speeds, in the direction of  $u$ , of  $v$  and  $w$ .

(i) Prove or verify that  $u + v = w$ .

(ii) If  $R = (u-v)/u$ , prove  $R = mw/(Mu)$ .

(iii) Express  $R$  in terms of  $M$  and  $m$  only.

[8]

### R1-2012 Q1(d)

- (d) A proton travelling with a velocity of  $3.00 \times 10^7 \text{ m s}^{-1}$  collides with an oxygen nucleus, of mass  $2.56 \times 10^{-26} \text{ kg}$  that is at rest, and is scattered through an angle of  $90^\circ$ . Calculate the velocity and direction of the oxygen nucleus using Newtonian mechanics.

[12]

### R1-2013 Q1(m)

- (m) A smooth flat horizontal turntable  $4.0 \text{ m}$  in diameter is rotating at  $0.050$  revs per second. A student at the centre of the turntable, and rotating with it, releases a smooth flat puck on the turntable  $0.50 \text{ m}$  from the edge. Describe the motion of the puck as seen by a stationary observer who is standing at the side of the turntable.

(i) How long does the puck remain on the turntable?

(ii) At what relative *velocity* would the student, at the centre of the turntable, see the puck leave the turntable?

[10]

## R1-2004 Q2

- a) A stone is dropped into a deep canyon. After 10.2 s it is heard to strike bottom. Estimate approximately:
- (i) the depth of the canyon,  $h$ , neglecting the time taken by the sound wave to return to the top of the canyon
  - (ii) the time  $t_2$  taken by the returning sound wave to reach the top of the canyon, assuming the speed of sound is  $334 \text{ m s}^{-1}$
  - (iii) the accuracy of the result in (i)
- [6]
- b) If  $t_1$  is the time taken for the stone to reach the bottom of the canyon and  $t_2$  is the time for the sound wave produced to reach the top of the canyon:
- (i) write down the equations that determine  $t_1$  and  $t_2$ , neglecting air resistance
  - (ii) calculate the exact value of  $t_1$
  - (iii) calculate the exact value of  $t_2$
  - (iv) deduce the depth of the canyon
- [10]
- c) If the stone is initially thrown with velocity  $u$  horizontally into the canyon, what differences will arise in the answers to question (b)(i)?
- [2]
- d) If the stone is thrown vertically upwards with velocity  $u$ , how will this alter the answers to question (b)(i)?
- [2]

## R1-2004 Q8

- a) Fast neutrons, mass  $m_1$ , with a speed  $v_1 = 2.0 \times 10^7 \text{ ms}^{-1}$ , are slowed down in a nuclear reactor by elastic collisions with the nuclei of a moderator. Calculate the speed  $v$  of a neutron after a single, head on, collision with (i) a hydrogen nucleus in water and (ii) a carbon nucleus in graphite by first deriving  $v$  in the general case of a collision with a nucleus of mass  $m_2$ . These nuclei are initially stationary.

After many collisions with atoms of a moderator at room temperature, what energy will the neutrons attain? The masses involved are:

neutron 1.0087 u; hydrogen nucleus 1.0073 u; carbon nucleus 11.9934 u

[12]

- b) The ballistic pendulum is a device used to measure the speed  $v$  of a bullet. It consists of a stationary heavy rectangular wooden block of mass  $M$  suspended by vertical strings from the corners of the upper horizontal face. When a bullet of mass  $m$  strikes the block horizontally it undergoes an inelastic collision and embeds itself in the block. The block swings upwards. If the block rises a height  $h$ , obtain an expression for the speed of the bullet assuming  $h$  is small and the block moves initially with a horizontal velocity.

Comment on the motion of the block during its upward swing.

[8]



## R1-2006 Q7

- (a) A projectile, mass  $m$ , is thrown vertically upwards with velocity  $v$ . Calculate:
- the maximum height,  $H$ , reached.
  - the time taken,  $T$ , to return to the ground.
- [2]
- (b) A horizontal wind exerts a horizontal force on the projectile of  $amg$ , where  $a$  is a constant. The projectile has initial vertical and horizontal components of velocity  $v$  and  $u$  respectively;  $u$  being taken in the same direction as the wind.
- What is the resultant force on the mass?
  - Determine the horizontal range,  $R$ , of the projectile.
  - Sketch the trajectory, indicating any axis of symmetry and giving its direction.
  - Under what initial condition, with the wind present, will the trajectory be a straight line? Give the elevation of this trajectory.
- [11]
- (c) Determine the work done *on* the mass during its motion:
- from its initial position to the maximum height in the case of a straight line trajectory.
  - for the general trajectory, from launch to its return to the ground.

[7]

### R1-2008 Q4(b)

(b)

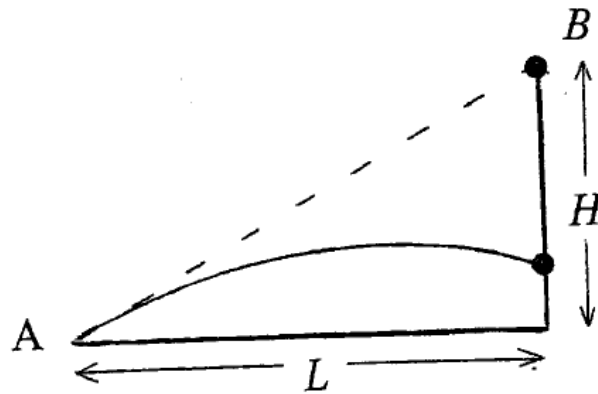


Figure 4.b

A marksman on the ground at A fires his rifle in the direction of a stationary clay pigeon located in a tower at B, height  $H$ , at a horizontal distance  $L$  from A, Figure 4b. At this instant the pigeon is released and falls vertically, under gravity. Verify that the bullet strikes the pigeon during its fall.

[12]

### R1-2008 Q5(a)

(a)

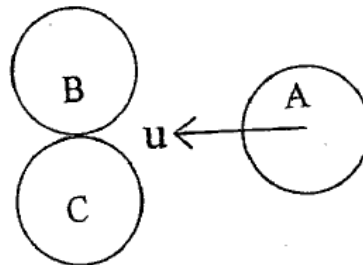


Figure 5.a

A sphere A travelling horizontally on a smooth table, with speed  $u$ , collides symmetrically, and elastically, with two stationary spheres, B and C, that are touching. All the spheres are identical and of mass  $m$ , Figure 5a. Determine the velocities of all the spheres after the collision.

C has a further collision with an identical sphere D, initially at rest and touching it. The centres of B, C and D lie on a straight line. Determine the outcome of this collision.

[12]

## R1-2009 Q2

A spherical stone is dropped from the top of a cliff of height  $h$  at time  $t = 0$ . At the same moment another identical stone is thrown vertically upwards from the bottom of the cliff with a *positive* velocity  $u$  in the same vertical line as the first stone.

- (a)
- (i) After what time,  $T_c$ , will the stones collide ?
  - (ii) If the stones have equal speeds on collision, what is the value of  $u$ , and  $T_c$  ?
  - (iii) If the collision in (ii) is elastic, determine the time interval between the impacts of the stones on the ground.

[9]

- (b)
- (i) Sketch a fully *labelled* velocity – time graph for the motion of the two stones, on the same graph, using a full curve for the stone dropped from the cliff top and a dotted curve for the stone projected vertically upwards from the bottom of the cliff.
  - (ii) Sketch a fully *labelled* height– time graph for the two stones using the notation specified in (i).

[11]

## R1-2011 Q4

- a) A stone is projected with a speed  $u$  at a small angle  $\alpha$  to the horizontal ground. It impacts on the ground at a distance  $d$ , having reached a maximum height  $h$ . At time  $t$  its velocity makes an angle  $\theta$  with the horizontal.

Determine in terms of  $u$  and  $\alpha$ :

- (i) The time taken,  $T_g$ , to reach the ground and the distance  $d$ .
- (ii) The maximum height,  $h$ , reached.
- (iii) An expression for the radius of curvature of the trajectory,  $R$ , at height  $h$ .
- (iv) Express  $R$  in terms of  $d$  and  $h$ .
- (v) Sketch a graph of  $\tan\theta$  against  $t$ , indicating the key points on the graph.
- (vi) Deduce, from (v), that there are no pair of points on the stone's trajectory, with velocities that are perpendicular if  $\alpha$  less than  $45^\circ$ .

[16]

- b) A car, mass  $m$ , travels across a parabolic bridge of horizontal length  $d$  and maximum height  $h$ , the same values as in (a), at a constant speed  $v$ . Determine the reaction force,  $N$ , exerted by the bridge on the car at height  $h$  for any value of  $v$ . What advantage could be obtained by adding a spoiler to the car?

[4]

## R1-2012 Q6

- (a) A block of wood, mass  $M$ , rests on a smooth horizontal table. A gun is fired horizontally at the block and the bullet, mass  $m$ , passes through it, emerging with half its initial speed. Determine the fraction of the initial kinetic energy that is lost in the collision.

[5]

- (b) A particle, mass  $m$ , is placed at the top of a smooth sphere of radius  $a$ . The particle is disturbed and slides down the side gaining speed  $v$  at a vertical height  $z$  above the centre of the sphere. At what value of  $z$  will it leave the surface of the sphere?

[6]

- (c) Figure 6.c shows two  $45^\circ$  wedges, the smaller wedge  $w$  has a horizontal top face. It can slide down the larger wedge  $W$ , which is on a horizontal table. All the surfaces are smooth. A mass  $m$  sits on the top face of the upper wedge. Describe qualitatively the motion of the system once it is released from rest.

[4]

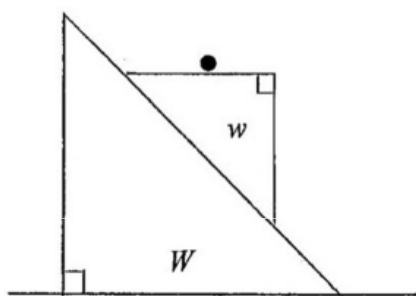


Figure 6.c

- (d) Two trains are travelling away from a common station at speeds of  $u$  and  $2u$ , in directions that are at an angle  $60^\circ$  to each other. What is the *velocity* of the train with speed  $2u$  relative to an observer in the other train?

[5]

## R1-2013 Q6

Three small identical steel balls A, B, and C are suspended by vertical threads of equal length from a horizontal support, with their centres in a horizontal line and separated by a small gap. A is raised by a height  $h$ , with the thread taut, and released. All subsequent collisions are elastic.

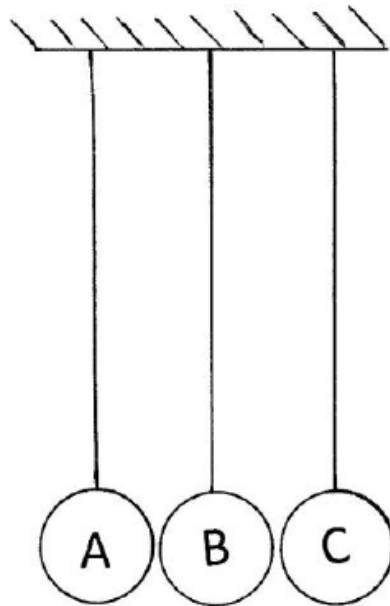


Figure 6.1

- (i) When all the balls have mass  $M$ , determine the subsequent motion of the system and the height to which the centre of C is raised following its first collision.

[8]

- (ii) When A has mass  $M$ , B has mass  $2M$  and C has mass  $3M$ , determine the height to which the centre of C is raised after its first collision.

[12]