

BRITISH PHYSICS OLYMPIAD 2014-15

A2 Challenge Solutions

- 1 a) i) Momentum
ii) mgh $\sqrt{(2gh)}$
iii) mgh h
- b) i) $\sqrt{(2gh)}$, downwards
ii) $\sqrt{(2gh)}$, upwards $2\sqrt{(2gh)}$
iii) $2\sqrt{(2gh)}$ $3\sqrt{(2gh)}$
iv) $9h$
- c) Speed after falling 1m = $\sqrt{(2gh)} = \sqrt{(2 \times 10 \times 1)} = 4.47 \text{ms}^{-1}$

By the reasoning above, successive balls will rise at $3\sqrt{(2gh)}$, $7\sqrt{(2gh)}$, $15\sqrt{(2gh)}$, $31\sqrt{(2gh)}$, $63\sqrt{(2gh)}$, $127\sqrt{(2gh)}$, $255\sqrt{(2gh)}$, $511\sqrt{(2gh)}$, $1023\sqrt{(2gh)}$, $2047\sqrt{(2gh)}$, $4095\sqrt{(2gh)}$ etc (spot that the coefficients 'double+ 1' each time)

As escape velocity is 2460 times 4.47ms^{-1} , 12 balls are required to reach escape velocity (Proposition not changed by use of $g=9.81 \text{ms}^{-2}$)

TOTAL 14

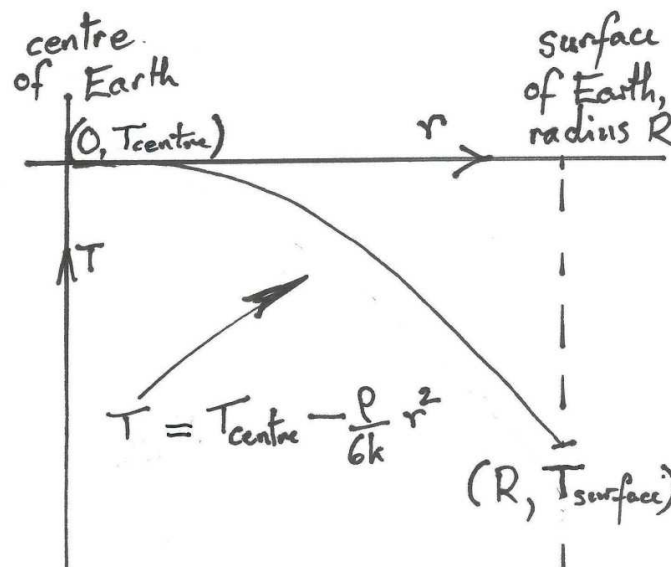
- 2 a) i) zero
ii) a node
iii) π or anything suggesting anti-phase (to give zero resultant displacement)
 $0, 2\pi$ or anything suggesting in phase
 $\pi, 3\pi, (2n+1)\pi$ or anything else suggesting anti-phase
- b) i) virtual
ii) both S, S' originate from same source and therefore must have a fixed phase difference **owtte**
iii) Light does not go on that side of the reflector
iv) $\lambda = xd/L$ = $10^{-3} \times 5 \times 10^{-4} / 1.00 = 5 \times 10^{-7} \text{m}$
v) Reflection introduces an extra phase difference of π , in addition to zero phase difference arising from geometrical p.d. , so central fringe is dark/ zero intensity **owtte**
vi) The zero-order in Young's fringes (with normal incidence) is an interference maximum. **owtte**

TOTAL 13

- 3 a) i) $1/R = 1/R_1 + 1/R_2$ **owtte** ✓
 ii) correct re-arrangement to give $R = R_1 R_2 / (R_1 + R_2)$ ✓
- b) i) 40Ω ✓
 ii) $((40+20) \parallel 20)$ ✓ (parallel part) + 20 = 35Ω ✓
 iii) Now this becomes $((r+20) \parallel 20) + 20$ realise this ✓
 ie $\frac{20(r+20)}{r+40} + 20 = \frac{40r+1200}{r+40}$ **owtte** ✓
 iv) Equating this to r ✓ and solving ✓ leads to $r = 20\sqrt{3}\Omega$

TOTAL 9

- 4 a) i) temperature higher than surroundings ✓
 ii) As thermal energy travels down temperature gradient, ✓
 Earth gets hotter towards centre. **owtte** ✓
 iii) $4\pi r^3 \rho / 3$ ✓
 iv) Area of shell is $4\pi r^2$, ✓
 so total power output is $(4\pi r^2) \times (-k \delta T / \delta r) = 4\pi r^3 \rho / 3$ ✓
 Rearranging gives $\delta T = -(\rho / 3k) r \delta r$ ✓
 v) Integrating wrt r ✓ and using $T = T_{centre}$ when $r = 0$ ✓
 Leads to $T = T_{centre} - \rho r^2 / 6k$ ✓
 vi)



Falls between centre and surface ✓
 Parabolic form with vertex correctly placed ✓

- b) They are much hotter in the centre than at the surface and may therefore reach ignition temperature. **owtte** ✓
 Breaking such a hot and occluded body of combustible material open exposes it to air richer in oxygen which can cause it to erupt violently into flames. **owtte** ✓

TOTAL 14