## British Physics Olympiad Paper 1: Solutions

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## Mark Scheme

Allow ecf where this gives sensible answers
Q1.
(a) The mass is simply the sum of the two individual masses i.e. 97 kg
(b)
i) Diagram of the form:

ii) 5 V drop across 0.2 Wresistor
leads to a current of 25 A maximum
So power available at 225 V is 5.63 kW
(4 marks)
(c)
i) Sound energy $=0.1 \times \mathrm{mgh}=0.1 \times 2 \times 10^{-4} \times 9.8 \times 1$

$$
=2 \times 10^{-4} \mathrm{~J}
$$

ii) Assume (maybe implicit) - Energy is spread over half of a sphere Or allow for whole sphere and energy absorbed by ground But some comment should be made about the assumption

$$
\begin{aligned}
\text { Ear receives energy } & =2 \times 10^{-4} \times \frac{\pi\left(6 \times 10^{-3}\right)^{2}}{4} / \frac{1}{2} 4 \pi 5^{2} \\
& =3.6 \times 10^{-11} \mathrm{~J}
\end{aligned}
$$

(d) An image is formed on the screen $(\checkmark)$ and your eye now focuses rays of light which come from each point on the screen to form a new image. A mirror would direct rays from the room to your eye from other parts of the room. $(\checkmark)$
(e) There are several approaches:

For (a), since $E=V / d$ then $E$ halves (as $d$ doubles), so $Q$ halves, $V$ is constant and hence energy stored halves.

For (b), $Q$ is constant, so $E$ is constant, so $V$ doubles
For constant $Q$ then the energy doubles
Ratio is $1: 4$
allow marks if answer given (not guessed)
(f) Amplitude $\rightarrow$ amplitude/4, so energy $\rightarrow$ energy/16

This is four half lives so time taken is 8.0 seconds, i.e. 1800 oscillations (ecf)
(g)
i) Archimedes upthrust/weight of the liquid displaced/etc.
ii) Sketch:

iii) By similar triangles:

$$
\frac{R}{r}=\frac{h}{\ell}
$$

iv) From the forces: weight of cone = weight of liquid displaced

$$
\begin{aligned}
& \rho_{c} \frac{1}{3} \pi R^{2} h g=\rho_{w} \frac{1}{3} \pi r^{2} \ell g \\
& \text { substituting for } \frac{h}{\ell} \\
& \rho_{c} h^{3}=\rho_{w} \ell^{3} \\
& \frac{\rho_{c}}{\rho_{w}}=\left(\frac{\ell}{h}\right)^{3}
\end{aligned}
$$

(h) i) Frequency remains the same the speed increases (as the ray bends away from the normal) wavelength increases
iii) Diagram of the form shown below, or with semicircles emerging or any alternative clear and reasonable interpretation

iii) $\quad$ minimum $d$ is $d_{\text {min }} \approx \lambda / 2$ orientation: the two waves are collinear with the centres of the speakers
(i) Angles shown to indicate angle $\mathrm{q}_{\mathrm{e}}$ with angle of $102^{\circ}$ inside the glass - 3 marks

Or statement that emerging ray is "above" the normal justified
Two marks for suitable correct rays and angles

(j) Field increases as $1 / r^{2}$. So calculation is

$$
\begin{aligned}
& \frac{B_{1}}{B_{2}}=\frac{R_{2}^{2}}{R_{1}^{2}} \\
& \frac{10^{-2}}{B_{2}}=\frac{(10)^{2}}{\left(1.4 \times 10^{6}\right)^{2}} \\
& B_{2}=10^{-2} \times 10^{-2} \times 1.96 \times 10^{12} \\
& B_{2}=2.0 \times 10^{8} \mathrm{~T}
\end{aligned}
$$

Right idea $\checkmark$, numbers substituted $\checkmark \checkmark$, answer $\checkmark$
(4 marks)
[Q1: 38]
Q2.
i) $\quad m=$ const $\times v^{a} \times g^{b} \times \rho^{c}$
(1 mark)
ii) The dimensions are given by

$$
[v]=\mathrm{LT}^{-1}, \quad[g]=\mathrm{L} \mathrm{~T}^{-2}, \quad[\mathrm{r}]=\mathrm{ML}^{-3}
$$

So then we can write

$$
\mathrm{M}=\left(\mathrm{LT}^{-1}\right)^{\mathrm{a}} \times\left(\mathrm{LT}^{-2}\right)^{\mathrm{b}} \times\left(\mathrm{ML}^{-3}\right)^{\mathrm{c}}
$$

iii) The powers of $\mathrm{M}, \mathrm{L}, \mathrm{T}$ on each side of the equation must be the same

For $\mathrm{M}: \quad \mathrm{M}^{1}=\mathrm{M}^{\mathrm{c}}$ so that $\mathrm{c}=1$
For $\mathrm{L}: \mathrm{L}^{0}=\mathrm{L}^{\mathrm{a}+\mathrm{b}-3 \mathrm{c}}$ so that $\mathrm{a}+\mathrm{b}-3 \mathrm{c}=0$
For $T: \quad T^{0}=T^{-a-2 b}$ so that $-a-2 b=0$
$b=-3$ and $a=6$
(4 marks)
iv)

$$
\begin{aligned}
& m=\text { const } \times v^{6} \times g^{-3} \times \rho \\
& \text { or } \quad \text { all correct: } \\
& m=\text { const } \frac{v^{6} \rho}{g^{3}}
\end{aligned}
$$

v) The high power of $v$ means that for a small increase in $v$ there will be a relatively large increase in $v^{6}$. owtte

